

30

Circuit Analysis

082 083 084

081

Circuit Analysis

by Prof. Dr. Osman SEVAİOĞLU Electrical and Electronics Engineering Department



What is an Electrical Circuit ?

Definition

An electrical circuit is a set of various system elements connected in a certain way, through which electrical current can pass







Thevenin Equivalent of an Electrical Circuit





Calculation of Thevenin Equivalent of a Circuit





Calculation of the Thevenin Equivalent Voltage Vequiv





Calculation of the Thevenin Equivalent Voltage Vequiv





Determination of Thevenin Equivalent Circuit by Calculation





Calculation of Thevenin Equivalent Resistance Requiv





Calculation of Thevenin Equivalent Resistance Requiv





Calculation of Thevenin Equivalent Resistance Requiv





Calculation of Thevenin Equivalent Resistance Requiv

4. Perform simplifications on the resulting circuit in order to find R_{equiv.}

 $R_{equiv} = ((R_3 // R_4) + R_1) // R_2$ = ((R_3 x R_4)/(R_3 + R_4) + R_1) // R_2 ((R_3 x R_4)/(R_3 + R_4) + R_1) x R_2 = ((R_3 x R_4)/(R_3 + R_4) + R_1) + R_2





Resulting Thevenin Equivalent Circuit





Example





Example





Example





Determination of the Thevenin Equivalent Circuit by using <u>Open and Short Circuit Tests</u>





Short Circuit Test





Open Circuit Test

Objective The main objective of Open Circuit Test is to determine the voltage at the terminals A and B when these terminals are open circuited



Procedure

- a) Open circuit the terminals of the given circuit,
 b) Measure the voltage V_{oc}
- between the terminals A and B of the given circuit





Determination of the Thevenin Equivalent Circuit by using Open and Short Circuit Tests





Example

Calculate the value of the unknown resistance R_x in the <u>unbalanced</u> Wheatstone Bridge shown on the RHS, if the current read by the ammeter is 5 Amp.

Since 5 Amp passes through the ammeter, the bridge is unbalanced, hence, cross multiplication of branches are not equal Please note that the bridge is <u>unbalanced</u>, i.e. current flows in the ammeter





Solution

First, take out the ammeter and 50 Ohm resistance connected to terminals C and D





Solution

Determine the Thevenin Equivalent of the source side of the circuit, i.e. the rest of the circuit after the ammeter and 50 Ohm resistance are taken out

1. Kill all the sources in the given circuit

Meaning of the The Term: "Killing Sources"

Means Short Circuiting the voltage source in the circuit on the RHS





Solution

Determine the Thevenin Equivalent of the source side of the circuit, i.e. rest of the circuit after the ammeter and 50 Ohm resistance are taken out

2. Calculate the equivalent resistance of the rest of the circuit









Solution

Determine the Thevenin Equivalent of the source side of the circuit, i.e. the rest of the circuit after the ammeter and 50 Ohm resistance are taken out

 $\begin{aligned} R_{eq} &= R_{eq1} + R_{eq2} \\ &= (R_{\chi} / / R_b) + (R_1 / / R_2) \\ &= (R_{\chi} \times 100) / (R_{\chi} + 100) + (100 \times 20) / (100 + 20) \end{aligned}$









Example 1. Unbalanced Wheatstone Bridge Solution Thevenin Equivalent Voltage **Input Voltage Determine the Thevenin Equivalent of** $V_{OC} = V_C - V_D$ the source side of the circuit, i.e. the rest of the circuit after the ammeter Α and 50 Ohm resistance are taken out **Restore back the source,** 2. $R_1 = 100 \Omega$ 3. **Open circuit the terminals C and** D and calculate the Thevenin **Equivalent Voltage** Vs Vc $V_{\rm c} = 100 \ V \times 100 \ /(100 + R_{\rm y})$ < R₂ = 20 Ω $R_{\rm h}$ = 100 Ω $V_{\rm D} = 100 \, \mathrm{V} \, x \, 20 \, / \, (100 + 20)$ $V_{\rm OC} = V_{\rm C} - V_{\rm D} = 100 \ (100/(100 + R_{\rm x}) - 100/6)$ Β







Example

Calculate the source voltage V_s by using the Thevenin Equivalent Circuit of the <u>unbalanced</u> Wheatstone Bridge shown on the RHS

Since the bridge is unbalanced, cross multiplication of branches are <u>NOT</u> equal, hence 5 Amp passes through the ammeter Please note that the bridge is unbalanced, i.e. current flows in the ammmeter









Example 2. Unbalanced Wheatstone Bridge

Solution

Thevenin Equivalent Resistance







EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 32



Example 2. Unbalanced Wheatstone Bridge









Example 2. Unbalanced Wheatstone Bridge Solution Thevenin Equivalent Voltage Now, find the Thevenin Equivalent $V_{0C} = V_C - V_D$ Voltage at the terminals C and D Α Put back the source, 1. Open circuit the terminals C and D, 2. 3. **Calculate the Thevenin Equivalent** Voltage at the terminals C and D **R**₁ Vs $V_c = V_s 100 / (100 + 50) = (2/3) V_s$ $V_D = V_s \times 20 / (100 + 20) = (2 / 12) V_s = V_s / 6$ ۶V_c Input $V_{OC} = V_C - V_D = V_s (2/3 - 1/6) = V_s / 2$ Volts Voltage Β






Norton Equivalent Circuit





Determination of Norton Equivalent Circuit Parameters





Example





Current Injection Model





Maximum Power Transfer Condition





Maximum Power Transfer Condition





Mathematical Fact

Mathematical Fact

A function passing through zero at two distinct points possesses at least one extremum point in the region enclosed by these points



Graphical Illustration



Maximum Power Transfer Condition

Graphical Representation

$P = R_L \times I^2 = R_L \times (V_{equiv} / (R_{equiv} + R_L))^2$

Thevenin Equivalent Circuit



EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 44



Maximum Power Transfer Condition

Solution: Then maximize; $P = R_L I^2$	Thevenin Equivalent Circuit
$P = R_L l^2$ $l^2 = (V_{eq} / R_{total})^2 = (V_{eq} / (R_{eq} + R_L))^2$ Hence, $P = R_L (V_{eq} / (R_{eq} + R_L))^2$ $= V_{eq}^2 R_L / (R_{eq} + R_L)^2$ Now, maximize P wrt R _L , by differentiating P with respect to R _L	$ \begin{array}{c} $
$\frac{dP}{dR_{L}} = 0$ $\frac{d/d}{R_{L}} \left(\frac{V_{eq}^{2} R_{L}}{R_{eq}^{2} R_{L}} \right) \left(\frac{R_{eq}^{2} R_{L}}{R_{eq}^{2} R_{L}} \right)^{2} = 0$ $\frac{V_{eq}^{2} \left[(R_{eq}^{2} + R_{L})^{2} - 2 (R_{eq}^{2} + R_{L}) R_{L} \right] / denom^{2} = 0$ where, denom = $(R_{eq}^{2} + R_{L})^{2}$ or $(R_{eq}^{2} + R_{L})^{2} - 2 (R_{eq}^{2} + R_{L}) R_{L}^{2} = 0$ $R_{eq}^{2} = R_{L}$	Conclusion:For maximum power transfer, load resistance R_L must be equal to the Thevenin Equivalent Resistance of the simplified circuit $R_{eq} = R_L$



Maximum Power Transfer Condition

Why do we need Maximum Power ?

Maximum power means maximum performance and maximum benefit by using the same equipment, and investment,

in other words, maximum speed, or maximum force, or maximum heating, or maximum illumination or maximum performance by using the same equipment, the same weight, and the same investment

Shanghai Maglev Train (World's Fastest Train)





Node (Junction)





Ground Node (Earth Point)





Ground Node (Earth Point)





What do we mean by Solution of an Electrical System?

Solution of an electrical system means calculation of all node voltages





Node Voltage Method

Procedure

- 1. Select one of the nodes in the system as the reference (usually the ground node), where voltage is assumed to be zero,
- 2. Convert Thevenin Equivalent circuits into Norton Equivalent circuits by;
 - Converting source resistances in series with the voltage sources to admittances in parallel with the current sources (injected currents)

 $g_{\rm s}=1/R_{\rm s}$

• Converting voltage sources to equivalent current sources, i.e. to equivalent current sources in parallel with admittances,

$$I_s = V_s / R_s = V_s g_s$$





Node Voltage Method

Procedure (Continued)

- 3. Assign number to each node,
- 4. Assign zero to ground node, as node the number,
- 5. Assign voltages $V_1, ..., V_{n-1}$ to all nodes except the ground (reference),
- 6. Set the voltage at the ground node to zero, i.e. $V_0 = 0$,

Please note that all these points form a single node





Sending end

Node Voltage Method

Procedure (Continued)

- 7. Assign current directions in all branches. (Define the direction of currents in the branches connected to the ground node as always flowing towards the ground),
- 8. Write-down branch currents in terms of the node numbers at the sending and receiving ends, where the sending and receiving ends are defined with respect to the current directions as defined above and as shown below,



 $I_{1-2} = (V_1 - V_2) / R_{12} = (V_1 - V_2) g_{12}$ $I_{1-0} = (V_1 - V_0) / R_{10} = V_1 g_{10}$ $I_{1-0s} = (V_1 - V_0) / R_s = V_1 g_s$ $I_{2-0} = (V_2 - V_0) / R_{20} = V_2 g_{20}$

EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 53

Receiving end



Node Voltage Method

Procedure (Continued)

9. Express branch currents in terms of the voltages at the sending and receiving ends by using Ohm's Law, except those flowing in the current sources (They are already known)



 $I_{1-2} = (V_1 - V_2) / R_{12} = (V_1 - V_2) g_{12}$ $I_{1-0} = (V_1 - V_0) / R_{10} = V_1 g_{10}$ $I_{1-0s} = (V_1 - V_0) / R_s = V_1 g_s$ $I_{2-0} = (V_2 - V_0) / R_{20} = V_2 g_{20}$



Node Voltage Method

Procedure (Continued)

 10. Write down KCL at all nodes except the ground (reference) node. (<u>Do not write KCL equation for the</u> ground node !)

Please note that there are only two unknown voltages, i.e. V_1 and V_2 Hence, KCL equations must be written only at these nodes, i.e. at nodes 1 and node 2

$$I_{s} = I_{1-0s} + I_{1-0} + I_{1-2}$$
$$I_{1-2} = I_{2-0}$$

Total no. of equations = N - 1

Number of nodes = N = 3 Number of equations = N-1 = 2





Node Voltage Method







Node Voltage Method





Node Voltage Method





Node Voltage Method





A Simple Rule for Forming Nodal Admittance Matrix



$g_{12} = 1 / R_{12}$

- Put the summation of admittances of those branches connected to the i-th node to the i-th diagonal element of the nodal admittance matrix
- Put the negative of the admittance of the branch connected between the nodes i and j to the i - jth and j-ith element of the nodal admittance matrix





A Simple Rule for Forming Node Voltage Vector





A Simple Rule for Forming Current Injection Matrix





Solution of Nodal Equations





Solution of Nodal Equations





Calculation of Inverse of a 2x2 Matrix

Procedure (Continued)

To find the inverse of a 2 x 2 matrix

1. First calculate the determinant of the given matrix;

Determinant = $a_{11} \times a_{22} - a_{21} \times a_{12}$ = d





Calculation of Inverse of a 2x2 Matrix

Procedure (Continued)

To find the inverse of 2 x 2 matrix

- 2. Then, calculate the co-factor matrix. To calculate the a_{11} element of the co-factor matrix;
 - Delete the 1st row and 1st column of the matrix,
 - Write down the remaining element a₂₂ in the diagonal position: 2,2, where the deleted row and column intercepts,





Calculation of Inverse of a 2x2 Matrix

Procedure (Continued)

To find the inverse of 2 x 2 matrix

- Perform the sam procedure for the next element a₁₂ in the matrix
- Repeat this procedure for all elements in A.





Calculation of Inverse of a 2x2 Matrix





Calculation of Inverse of a 2x2 Matrix





Example





Example (Continued)

Procedure (Continued)

To find the inverse of 2 x 2 matrix

- 2. Then, calculate the co-factor matrix. To calculate the a_{11} element of the co-factor matrix;
 - Delete the 1st row and 1st column of the matrix,
 - Write down the remaining element a₂₂ in the diagonal position: 2,2, where the deleted row and column intercepts,





Example (Continued)

Procedure (Continued)

To find the inverse of 2 x 2 matrix

- Perform the sam procedure for the next element a₁₂ in the matrix
- Repeat this procedure for all elements in A.




Example (Continued)





Example (Continued)





Solution of Large - Size Systems





Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

Hence, we must find the inverse of the coefficient matrix G

To find the inverse of 3 x 3 matrix

- 1. First calculate the determinant of the matrix;
 - For that purpose, first augment the given matrix by the "first two"... columns of the same matrix from the RHS
 - Then, multiply the terms on the main diagonal





Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)	$\begin{bmatrix} a_{11} & a_{12} & a_{13} \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \end{bmatrix}$
 Then, multiply the terms on the other (cross) diagonal 	$\begin{bmatrix} a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} a_{21} & a_{22} \\ a_{31} & a_{32} \end{bmatrix}$
	$\begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{11} & a_{12} \\ a_{21} & a_{22} & a_{23} & a_{21} & a_{22} \\ a_{31} & a_{32} & a_{33} & a_{31} & a_{32} \end{bmatrix}$
	a ₁₃ x a ₂₂ x a ₃₁ a ₁₁ x a ₂₃ x a ₃₂ a ₁₂ x a ₂₁ x a ₃₃ a ₁₂ x a ₂₃ x a ₃₃



Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

• Then, subtract the latter three multiplications from those found in the former





Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

- 1. Then, calculate the co-factor matrix. To calculate the a_{ij} ^{-th} element of the co-factor matrix;
 - Delete the i the row and j the column of the matrix,
 - Calculate the determinant c_{ij} of the remaining 2 x 2 submatrix by using the method given earlier for 2 x 2 matrices





Calculation of Inverse of a 3x3 Matrix





Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

- Write down these determinants in the corresponding locations,
- Set the sign of these elements such that;

$$\begin{bmatrix} c_{11} & -c_{12} & c_{13} \\ -c_{21} & c_{22} & -c_{23} \\ c_{31} & -c_{32} & c_{33} \end{bmatrix}$$



Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

2. Then, transpose the resulting cofactor matrix

$$\begin{bmatrix} c_{11} & -c_{12} & c_{13} \\ -c_{21} & c_{22} & -c_{23} \\ c_{31} & -c_{32} & c_{33} \end{bmatrix}^{\mathsf{T}}$$

$$\begin{bmatrix} c_{11} & -c_{21} & c_{31} \\ -c_{12} & c_{22} & -c_{32} \\ c_{13} & -c_{23} & c_{33} \end{bmatrix}$$



Calculation of Inverse of a 3x3 Matrix





Example

Example

Find the inverse of the coefficient matrix given on the RHS

- 1. First calculate the determinant of the matrix;
 - For that purpose, first augment the given matrix by the "first two" columns of the same matrix from the RHS
 - Then, multiply the terms on the main diagonal





Example

Procedure (Continued)

• Then, multiply the terms on the other (cross) diagonal





Example

Procedure (Continued)

• Then, subtract the latter three multiplications from those found in the former





Example

Procedure (Continued)

- 1. Then, calculate the co-factor matrix. To calculate the a_{ij} ^{-th} element of the co-factor matrix;
 - Delete the i the row and j the column of the matrix,
 - Calculate the determinant c_{ij} of the remaining 2 x 2 submatrix by using the method given earlier for 2 x 2 matrices





Calculation of Inverse of a 3x3 Matrix





Calculation of Inverse of a 3x3 Matrix

Procedure (Continued)

- Form the co-factor matrix as shown on the RHS
- Transpose the co-factor matrix (It will not change since it is symmetrical)

$$= \begin{bmatrix} 12 & -12 & -36 \\ -12 & -14 & 10 \\ -36 & 10 & 4 \end{bmatrix}$$



Calculation of Inverse of a 3x3 Matrix





Solution Step

Procedure (Continued)

Final step of the solution procedure is the multiplying the RHS vector with the inverse of the nodal admittance matrix These elements are zero for nodes with no current injection









Procedure (Continued)

Sometimes we may encounter a <u>"Pure</u> <u>Voltage Source"</u> connecting two nodes other than ground.

This means that the voltage difference between these nodes is fixed

A pure voltage source with no series resistance creates problem in the solution procedure, since it cannot be converted to an equivalent Norton Equivalent Circuit, i.e.

 $V_{\rm s}/R_{\rm s} = V_{\rm s}/0 = \infty$





Procedure (Continued)

In this case, the circuit can be solved as follows

- Define the current flowing in this voltage source as I_x
- 2. Define this current as a new variable,
- 3. Write down KCL at each node, except the reference node,
- 4. Write down the equation for the voltage difference between the terminals of this pure voltage source















EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 97



Nodal Analysis with Controlled Sources

Nodal Analysis with Voltage Controlled Current Sources

Voltage Controlled Current Source: $I_s = A V_x$

Procedure

- Write down the expression for the current provided by the controlled current source in terms of the node voltage depended: I_s = A V₁
- Include this current in the summation when writing KCL for the node that controlled current source is connected,
- Solve the resulting nodal equations for node voltages





Nodal Analysis with Controlled Sources

Nodal Analysis with Current Controlled Current Sources

Current Controlled Current Source: $I_s = A I_x$

Procedure

- Write down the expression for the current provided by the controlled current source in terms of current depended: I_s = A I₁₋₀
- Express the depended current, I₁₋₀ and hence I_s in terms of node voltages;
 I_s = A (V₁ - V₀) / R₁₋₀ = A V₁ g₁₋₀
- Include this current in the summation when writing KCL for node that controlled current is injected,
- Solve the resulting nodal equations for node voltages





Nodal Analysis with Controlled Sources

Nodal Analysis with Current Controlled Voltage Sources

Current Controlled Voltage Source: $V_s = A I_x$

Procedure

- Write down the expression for the controlled voltage in terms of the current depended: $V_s = A I_{1-0}$
- Express the depended current, I₁₋₀ and hence V_s in terms of the node voltages,
- Convert the resulting voltage source V_s to equivalent Norton current source,
- Include this current in the summation when writing KCL for node that that controlled current is injected,
- Solve the resulting nodal equations for node voltages





Nodal Analysis with Controlled Sources

Nodal Analysis with Voltage Controlled Voltage Sources

Voltage Controlled Voltage Source: $V_s = A V_x$

Procedure

- Write down the expression for the controlled voltage in terms of the voltage depended: $V_s = A V_x = A V_1$
- Convert the resulting voltage source V_s to equivalent Norton current source,
- Include this current in the summation when writing KCL for node that controlled current is injected,
- Solve the resulting nodal equations for node voltages





Example

Node Voltage Method with Controlled Current Source

Find the power dissipated in the resistance R_L in the following circuit by using the <u>Node Voltage</u> <u>Method</u>



<u>Please note that current</u> <u>controlled current source</u> <u>in the circuit can NOT be</u> <u>killed for finding the</u> <u>Thevenin Equivalent Circuit</u>

If you do, the result will be INCORRECT !

Hence, simplification by employing Thevenin Equivalent Circuit Method is NOT applicable to this problem

Load Resistance $R_L = 1 \Omega$



Example (Continued)

Node Voltage Method with Controlled Current Source

The first step of the solution is to combine the resistances R_L and 1 Ohm yielding a 3 Ohm resistance, thus eliminating the third node





Example (Continued)



Equation - 1 $8V_2/3 - V_1/2 - V_1/1 - (V_1 - V_2)/4 = 0$



Example (Continued)

2

 $\downarrow I_{2-0}$

l_{s2} = 10 A

| |₃₋₀





Example (Continued)





Example (Continued)





Mesh Current Method




Mesh Current Method





Mesh Current Method





Mesh Current Method

Mesh

Please note that the path shown by dashed line is NOT a mesh, since it contains some other loops inside





Mesh Current Method

Procedure

1. Determine the meshes and mesh current directions in the circuit by following the rules;





Mesh Current Method

Procedure

- 2. Define mesh currents in each mesh flowing in the <u>clockwise direction</u>,
- 3. Convert all current sources with parallel admittances, if any, to equivalent Thevenin voltage sources with series Thevenin equivalent resistances,







Mesh Current Method

Procedure

- 4. Write down Kirchoff's Voltage Law (KVL) in each mesh in terms of the source voltages, mesh currents and resistances,
- 5. Solve the resulting equations





Mesh Current Method





Mesh Current Method





Mesh Current Method





Mesh Current Method





- R13

Circuit Analysis

Mesh Equations in Matrix Form



EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 119

 $R_{32} + R_{13} + R_{12}$

 $-R_{32}$



Mesh Current Method





Solution Step





Rules for Forming Mesh Resistance Matrix





- Put the summation of the resistances of branches in the ith mesh path to the ith diagonal location in the mesh resistance matrix,
- Put the negative of the resistance of branch which is common to both ith and jth meshes to the (i – j)th location of the mesh resistance matrix





Rules for Forming the Unknown (Mesh Current) Vector



in a sequence starting from 1 to n-1 (i.e. for all meshes in the circuit)





Rules for Forming the known (RHS) Vector





Example - 1





Example - 1



EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 126



Example - 2





Example - 2 (Continued)



To simplify the circuit, first convert the Northon Equivalent Circuit shown in the shaded area to Thevenin Equivalent Circuit



Example - 2 (Continued)



To simplify the circuit, further, combine the voltage sources and the 5 Ohm resistances



Example - 2 (Continued)





Example - 2 (Continued)





Example - 2 (Continued)





Procedure

Sometimes we may encounter a current source with no parallel admittance, called <u>"Pure Current Source"</u>

A pure current source connecting two nodes without any shunt admittance means that there is fixed difference between the mesh currents involving this current source

A pure current source with no shunt admittance creates problem, since it cannot be converted into an equivalent Thevenin form, i.e.

$$I_{\rm s} / g_{\rm equiv} = I_{\rm s} / 0 = \infty$$





Procedure

The circuit is solved as follows

- Define the voltage across the pure current source as V_x
- 2. Define this voltage (V_x) as a new variable,
- 3. Write down KVL for each mesh,
- 4. Write down the equation for the current difference between the meshes by using this pure current source











EE 209 Fundamentals of Electrical and Electronics Engineering, Prof. Dr. O. SEVAİOĞLU, Page 136



Supernode





The Principle of Superposition

WW MΛ Method SC Kill all the sources except one, • Solve the resulting circuit, • **≧**† I₂' **↓ |**₂ SC Restore back the killed source, • Kill another source, • ww \mathcal{M} Repeate this procedure for all sources, • SC Sum up all the solutions found • <u>5</u> V_{s1} ٨٨٨٨ ۸۸۸۸/ 00 **≩**↓ا₃ ≷↓I₄ **≦**†I₂" V_{s2} + **I**6 l, l₅____ S ww WW MM V_{s1} <u>∎</u>5 w ≶†I₂ I₃ ≷↓ I₄ SC ‴!†**≹** 16



Example





Star - Delta Conversion





Star - Delta Conversion





Delta - Star Conversion

Formulation

A set of delta – connected resistances can be converted to a star connection as shown on the RHS

$$R_{a} = R_{ba} R_{ac} / (R_{ba} + R_{ac} + R_{cb})$$
$$R_{b} = R_{cb} R_{ba} / (R_{ba} + R_{ac} + R_{cb})$$
$$R_{c} = R_{ac} R_{cb} / (R_{ba} + R_{ac} + R_{cb})$$





Delta - Star Conversion

In case that the resistances are identical, the equivalent star connection can further be simplified to the form shown on the RHS

Simplification

$$R_{Y} = R_{A}^{2} / (R_{A} + R_{A} + R_{A}) = R_{A} / 3$$

