



Course Title and Code Number:  
 Control Systems and Components (EE391)  
 Third Year (Communications and Electronics)  
 Time Allowed: 45 Mins

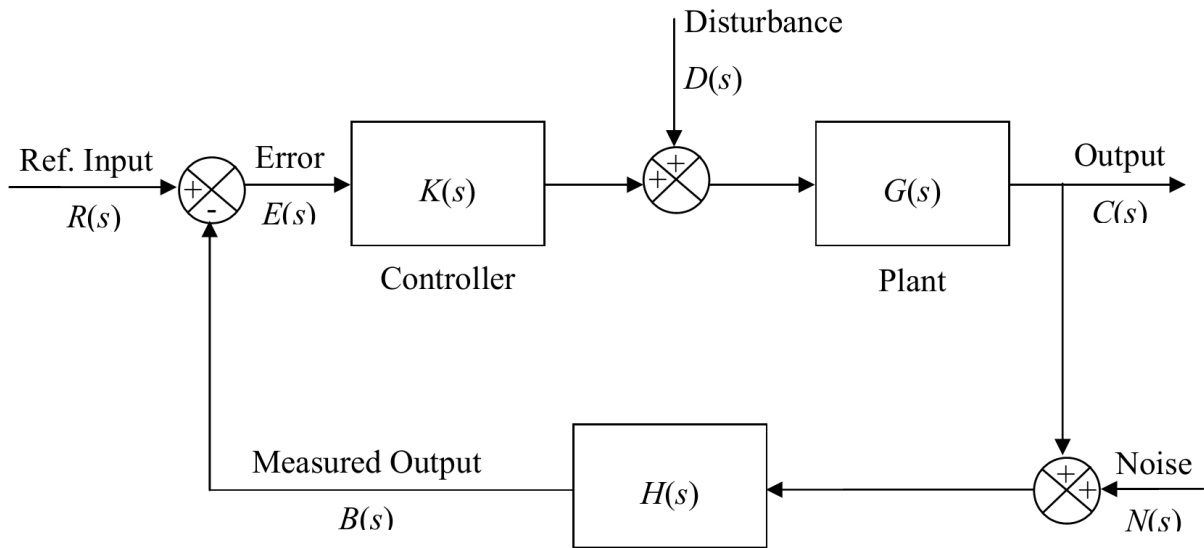
اسم المقرر والرقم الكودي له:  
 أنظمة التحكم ومكوناتها (EE391)  
 السنة الدراسية الثالثة (اتصالات و الكترونياات)  
 الزمن: ٤٥ دقيقة

**Answer All Questions:**

**(15 marks)**

**Laplace transform table is provided in page 2:**

1. The following block diagram represents a generic closed-loop linear system consisting of a reference input  $R(s)$ , a disturbance  $D(s)$ , and sensor noise  $N(s)$  and output  $C(s)$ . **(5 marks)**



**Figure 1**

- Evaluate the output  $C(s)$  in terms of the inputs  $R(s)$ ,  $D(s)$ , and  $N(s)$ .
- Assume that  $H(s) = 1$  (i.e. unity feedback) and  $K(s) = K$  (proportional controller). Assume also that there is no noise or disturbance (i.e.  $N(s) = 0$  and  $D(s) = 0$ ). Derive a simple expression for the error  $E(s) = R(s) - B(s)$ , in terms of  $R(s)$ ,  $G(s)$ , and  $K$ .
- Consider the following transfer function of the plant:

$$G(s) = \frac{1}{2 + s^2}$$

Assume  $H(s) = 1$ ,  $K(s) = K$ ,  $N(s) = 0$ , and  $D(s) = 0$ . Find the steady state error  $e_{ss}$  for a unit-step reference input  $R(s)$ , (i.e.  $e(t)$  as  $t$  goes to infinity).

2. Simplify the block diagram shown in Figure 2 and obtain the closed-loop transfer function  $C(s)/R(s)$ . (4 marks)

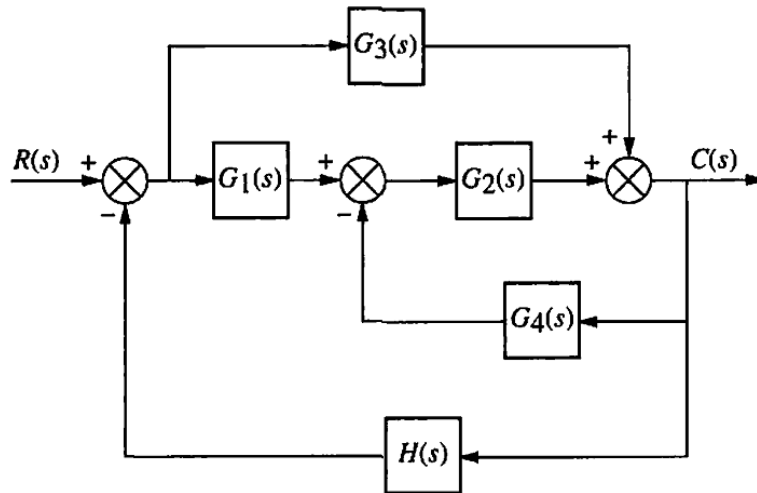


Figure 2

3. For the second-order system shown in Figure 3 (6 marks)
- Derive an expression of the output  $C(s)$  for a unit step input  $R(s)$ .
  - Derive an expression for the peak time, and maximum overshoot for the underdamped system.
  - Determine the values of  $K$  and  $B$  of the closed-loop system so that the maximum overshoot in unit-step response is 25% and the peak time is 2 sec. Assume that  $J=1\text{kg-m}^2$ .

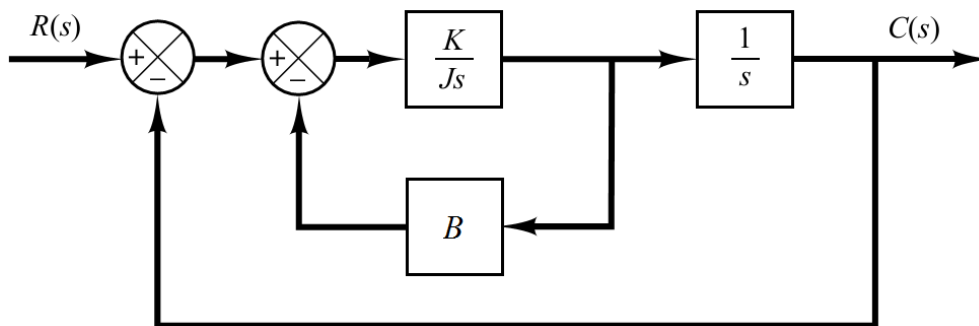


Figure 3

Table1 : Laplace Transform Pairs

$L[f(t)] \rightarrow F(s)$	$L[\sin(\omega t)] \rightarrow \frac{\omega}{s^2 + \omega^2}$	$L[\text{unit step } 1(t)] \rightarrow \frac{1}{s}$	$L\left(\frac{t^{n-1}}{(n-1)!}\right) \rightarrow \frac{1}{s^n}$
$L[\delta(t)] \rightarrow 1$	$L[\cos(\omega t)] \rightarrow \frac{s}{s^2 + \omega^2}$	$L(t) \rightarrow \frac{1}{s^2}$	$L[e^{-at} \cdot f(t)] \rightarrow F(s+a)$

Good Luck

Examiner: Dr. Mohammed Morsy