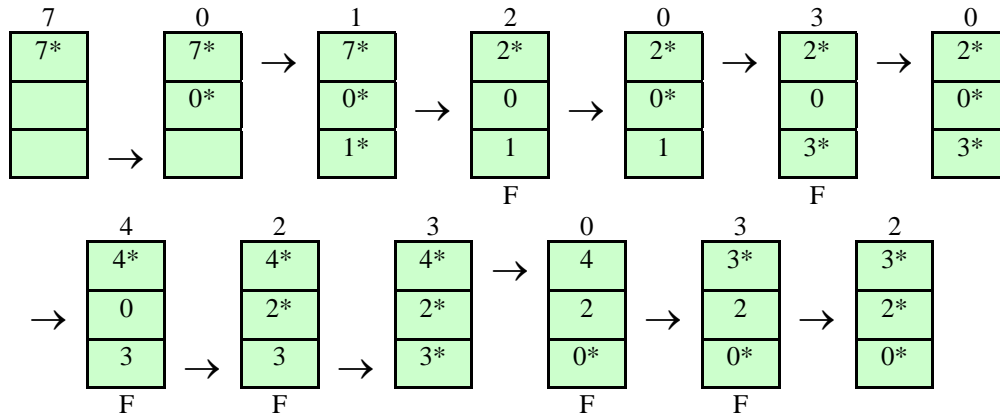


	0	0	0	0	0	0	0	0	3	3	3	3
		1	1	1	3	3	3	2	2	2	2	2
			F		F		F	F	F	F		

c) Clock



d) Optimal (assume the page reference string continues with 1, 2, 0, 1, 7, 0, 1)

7	0	1	2	0	3	0	4	2	3	0	3	2
7	7	7	2	2	2	2	2	2	2	2	2	2
	0	0	0	0	0	0	4	4	4	0	0	0
		1	1	3	3	3	3	3	3	3	3	3
			F		F					F		

e) List the total number of page faults and the miss rate for each policy. Count page faults only after all frames have been initialized.

FIFO: page faults = 7 miss rate = 70%

LRU: page faults = 6 miss rate = 60%

Clock: page faults = 6 miss rate = 60%

OPT: page faults = 3 miss rate = 30%

8) A process references five pages, A, B, C, D, and E, in the following order:

A; B; C; D; A; B; E; A; B; C; D; E

Assume that the replacement algorithm is first-in-first-out and find the number of page transfers during this sequence of references starting with an empty main memory with three page frames. Repeat for four page frames.

9 and 10 page transfers, respectively. This is referred to as "Belady's anomaly," and was reported in "An Anomaly in Space-Time Characteristics of Certain Programs Running in a Paging Machine," by Belady et al, Communications of the ACM, June 1969.

9) A process contains eight virtual pages on disk and is assigned a fixed allocation of four page frames in main memory. The following page trace occurs:

1, 0, 2, 2, 1, 7, 6, 7, 0, 1, 2, 0, 3, 0, 4, 5, 1, 5, 2, 4, 5, 6, 7, 6, 7, 2, 4, 2, 7, 3, 3, 2, 3

a) Show the successive pages residing in the four frames using the LRU replacement policy. Compute the hit ratio in main memory. Assume that the frames are initially empty.

Hit ratio = 16/33

```

1 0 2 2 1 7 6 7 0 1 2 0 3 0 4 5 1 5 2 4 5 6 7 6 7 2 4 2 7 3 3 2 3
1 1 1 1 1 1 1 1 1 1 1 1 1 1 4 4 4 4 4 4 4 4 4 4 2 2 2 2 2 2 2 2
- 0 0 0 0 0 6 6 6 6 2 2 2 2 2 5 5 5 5 5 5 5 5 5 5 4 4 4 4 4 4 4
- - 2 2 2 2 2 0 0 0 0 0 0 0 0 0 2 2 2 2 7 7 7 7 7 7 7 7 7 7 7
- - - - - 7 7 7 7 7 7 7 3 3 3 3 1 1 1 1 6 6 6 6 6 6 6 6 3 3 3 3
F F F      F F  F  F  F  F F F  F      F F      F F      F

```

b) Repeat part (a) for the FIFO replacement policy.

Hit ratio = 16/33

```

1 0 2 2 1 7 6 7 0 1 2 0 3 0 4 5 1 5 2 4 5 6 7 6 7 2 4 2 7 3 3 2 3
1 1 1 1 1 1 6 6 6 6 6 6 6 6 4 4 4 4 4 4 4 6 6 6 6 6 6 6 6 6 2 2
- 0 0 0 0 0 0 0 0 0 1 1 1 1 1 5 5 5 5 5 5 5 7 7 7 7 7 7 7 7 7 7
- - 2 2 2 2 2 2 2 2 2 0 0 0 0 0 1 1 1 1 1 1 1 1 1 4 4 4 4 4 4 4
- - - - - 7 7 7 7 7 7 7 3 3 3 3 3 3 2 2 2 2 2 2 2 2 2 2 2 3 3 3 3
F F F      F F      F  F F  F F F  F      F F      F      F  F

```

c) Compare the two hit ratios and comment on the effectiveness of using FIFO to approximate LRU with respect to this particular trace.

These two policies are equally effective for this particular page trace.

10) Consider a page reference string for a process with a working set of M frames, initially all empty. The page reference string is of length P with N distinct page numbers in it. For any page replacement algorithm,

a) What is a lower bound on the number of page faults?

N

b) What is an upper bound on the number of page faults?

P